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LL               II                    SSSSSS
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LL               II                    SS
LL               II                    SS
LLLLLLLLLLLLLL  IIIIII               SSSSSSSS
LLLLLLLLLLLLLL  IIIIII               SSSSSSSS

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(2) 55
(3) 90
(4) 182

HISTORY ; Detailed current edit history
DECLARATIONS
OT\$POWRR - REAL to REAL giving REAL result

```

0000 1      .TITLE  UVX$POWRR - REAL ** REAL power routine
0000 2      .IDENT  /2-008/      ; File: OTSPOWRR.MAR Edit: JCW2008
0000 3
0000 4
0000 5      *****
0000 6      *
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0000 23     *  SOFTWARE ON EQUIPMENT WHICH IS NOT SUPPLIED BY DIGITAL.
0000 24     *
0000 25     *
0000 26     *****
0000 27
0000 28
0000 29     FACILITY: Language support library - user callable
0000 30     ++
0000 31     ABSTRACT:
0000 32
0000 33         REAL base to REAL power.
0000 34
0000 35         Floating overflow can occur
0000 36         Undefined exponentiation can occur if:
0000 37             1) Negative base
0000 38             2) 0 base and power is 0 or negative.
0000 39
0000 40
0000 41     --
0000 42
0000 43     VERSION: 2
0000 44
0000 45     HISTORY:
0000 46
0000 47     AUTHOR:
0000 48         Bob Hanek, 3-Mar-83: Version 2
0000 49
0000 50     MODIFIED BY:
0000 51
0000 52         Jeffrey C. Wiener, 9-MAY-83: Version 2-002
0000 53

```



```
0000 55      .SBTTL HISTORY      ; Detailed current edit history
0000 56
0000 57
0000 58 : Edit history for Version 2 of OTSS$POWRR
0000 59 :
0000 60 : 2-001 New algorithm implemented. RNH 3-Mar-83
0000 61 : 2-002 Since microVAX requires that F floating point routines may only
0000 62 : be backed-up by G floating point instructions, the previous version
0000 63 : of this routine has been modified to accomplish this requirement.
0000 64 : JCW 9-MAY-83.
0000 65 : 2-003 Change INDEX table to be a local table rather than a GLOBAL table.
0000 66 : LEB 24-May-1983.
0000 67 : 2-004 Change reference of INDEX(Rx) to be INDEX[Rx] to avoid linker
0000 68 : errors. LEB 25-May-1983
0000 69 : 2-005 Changed MTH$POWRR entry to OTSS$POWRR entry. JCW 26-May-1983
0000 70 : 2-006 Change reference of A_TABLE(Rx) to be A_TABLE[Rx]. LEB 26-May-1983
0000 71 : 2-007 Added two ROTL #-3,Rx,Rx instructions to scale the value of Rx back
0000 72 : from 'index*2^3' to 'index' before A_TABLE[Rx] is referenced. The
0000 73 : INDEX was not scaled back to yield values of 'index' instead of
0000 74 : 'index*2^3' because the mathematics of the code used does need the
0000 75 : value of index*2^3 in several computations. JCW 7-Jun-1983
0000 76 : 2-008 Corrected two bugs. The first bug was the omission of an A_TABLE
0000 77 : entry for 2^(16/16). While doing this I also converted all the
0000 78 : A_TABLE entries so that they now represented rounded values, rather
0000 79 : than truncated values. This will increase accuracy. This was also
0000 80 : done for C0. The other bug involved a SYS_F FLT0VF_F error during
0000 81 : a MULG2 R0, R2. Code was added to see if a MTH overflow message or a
0000 82 : zero should be returned. While examining the code I also noticed that
0000 83 : the accuracy could be increased by replacing some of the CVTGF's (which
0000 84 : round) by code that would cause the CVTGF to truncate. The last CVTGF
0000 85 : in the code was not fixed in this manner because at this level in the
0000 86 : routine you are ready to return your result, which is always rounded
0000 87 : off. JCW 19-Jan-1984
0000 88 :
```

```
0000 90      .SBTTL  DECLARATIONS
0000 91
0000 92      :
0000 93      : INCLUDE FILES:
0000 94      :
0000 95      :
0000 96      :
0000 97      : EXTERNAL SYMBOLS:
0000 98      :
0000 99      : .DSABL  GBL
0000 100     : .EXTRN  MTH$K_UNDEXP      ; Undefined exponentiation
0000 101     : .EXTRN  MTH$K_FLOUNDMAT   ; Underflow
0000 102     : .EXTRN  MTH$K_FLOOVEMAT   ; Overflow
0000 103     : .EXTRN  MTH$$SIGNAL       ; Math error routine
0000 104     :
0000 105     : MACROS:
0000 106     :
0000 107     :     $$FDEF                  ; Define stack frame symbols
0000 108     :
0000 109     :
0000 110     : EQUATED SYMBOLS:
0000 111     :
00000004 0000 112     :     base      = 4      ; base input formal - by-value
00000008 0000 113     :     exp       = 8      ; exponent input formal - by-value
0000001C 0000 114     :     ACMASK    = ^M< R2, R3, R4> ; register saving mask
384F43F6 0000 115     :     C2       = ^X384F43F6
C0234393 0000 116     :     C4       = ^XC0234393
0000 117     :
0000 118     : OWN STORAGE:
0000 119     :
0000 120     :     none
0000 121     :
0000 122     :
0000 123     : PSECT DECLARATIONS:
0000 124     :
00000000 0000 125     :     .PSECT  _OTSS$CODE      PIC,SHR,LONG,EXE,NOWRT
0000 126     :                                     ; program section for OTS$ code
0000 127     :
0000 128     : CONSTANTS:
0000 129     :
0000 130     :
0000 131     :
0000 132     : The INDEX table gives the byte offset into the A_TABLE necessary to select
0000 133     : the proper choice of 'a.'
0000 134     :
008 08 08 08 08 00 00 00 0000 135 INDEX: .BYTE  ^X00, ^X00, ^X00, ^X08, ^X08, ^X08, ^X08, ^X08
18 10 10 10 10 10 10 08 0008 136      .BYTE  ^X08, ^X10, ^X10, ^X10, ^X10, ^X10, ^X10, ^X18
20 20 20 18 18 18 18 18 0010 137      .BYTE  ^X18, ^X18, ^X18, ^X18, ^X18, ^X20, ^X20, ^X20
28 28 28 28 20 20 20 20 0018 138      .BYTE  ^X20, ^X20, ^X20, ^X20, ^X28, ^X28, ^X28, ^X28
30 30 30 30 30 30 28 28 0020 139      .BYTE  ^X28, ^X28, ^X30, ^X30, ^X30, ^X30, ^X30, ^X30
38 38 38 38 38 38 30 30 0028 140      .BYTE  ^X30, ^X30, ^X38, ^X38, ^X38, ^X38, ^X38, ^X38
40 40 40 40 40 40 40 38 0030 141      .BYTE  ^X38, ^X40, ^X40, ^X40, ^X40, ^X40, ^X40, ^X40
48 48 48 48 48 48 48 40 0038 142      .BYTE  ^X40, ^X48, ^X48, ^X48, ^X48, ^X48, ^X48, ^X48
50 50 50 50 50 50 50 48 0040 143      .BYTE  ^X48, ^X50, ^X50, ^X50, ^X50, ^X50, ^X50, ^X50
58 58 58 58 58 58 50 50 0048 144      .BYTE  ^X50, ^X50, ^X58, ^X58, ^X58, ^X58, ^X58, ^X58
60 60 60 60 60 58 58 58 0050 145      .BYTE  ^X58, ^X58, ^X58, ^X60, ^X60, ^X60, ^X60, ^X60
68 68 68 68 60 60 60 60 0058 146      .BYTE  ^X60, ^X60, ^X60, ^X60, ^X68, ^X68, ^X68, ^X68
```



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70 70 68 68 68 68 68 68 0060 147 .BYTE ^X68, ^X68, ^X68, ^X68, ^X68, ^X68, ^X70, ^X70
70 70 70 70 70 70 70 70 0068 148 .BYTE ^X70, ^X70, ^X70, ^X70, ^X70, ^X70, ^X70, ^X70
78 78 78 78 78 78 78 78 0070 149 .BYTE ^X78, ^X78, ^X78, ^X78, ^X78, ^X78, ^X78, ^X78
80 80 80 80 80 78 78 78 0078 150 .BYTE ^X78, ^X78, ^X78, ^X80, ^X80, ^X80, ^X80, ^X80
0080 151
      832D652B 15474097 0080 152 C0: .QUAD ^X832D652B15474097
0088 153
0088 154
0088 155 : The ith entry of the A_TABLE contains the value 2^(i/16)
0088 156 :
0088 157
00000000 00004010 0088 158 A_TABLE: .QUAD ^X000000000000004010 : 2^( 0/16)
890F6CF9 B5584010 0090 159 .QUAD ^X890F6CF9B5584010 : 2^( 1/16)
517B3C7D 72B84011 0098 160 .QUAD ^X517B3C7D72B84011 : 2^( 2/16)
62386E75 387A4012 00A0 161 .QUAD ^X62386E75387A4012 : 2^( 3/16)
B7150A31 06FE4013 00A8 162 .QUAD ^XB7150A3106FE4013 : 2^( 4/16)
34224C12 DEA64013 00B0 163 .QUAD ^X34224C12DEA64013 : 2^( 5/16)
2A27D536 BFDA4014 00B8 164 .QUAD ^X2A27D536BFDA4014 : 2^( 6/16)
5429DD48 AB074015 00C0 165 .QUAD ^X5429DD48AB074015 : 2^( 7/16)
3BCD667F A09E4016 00C8 166 .QUAD ^X3BCD667FA09E4016 : 2^( 8/16)
018773EB A1144017 00D0 167 .QUAD ^X018773EBA1144017 : 2^( 9/16)
A0DB422A ACE54018 00D8 168 .QUAD ^XA0DB422AACE54018 : 2^(10/16)
F09082A3 C4914019 00E0 169 .QUAD ^XF09082A3C4914019 : 2^(11/16)
D3AD995A E89F401A 00E8 170 .QUAD ^XD3AD995AE89F401A : 2^(12/16)
529CDD85 199B401C 00F0 171 .QUAD ^X529CDD85199B401C : 2^(13/16)
A487DCFB 5818401D 00F8 172 .QUAD ^XA487DCFB5818401D : 2^(14/16)
90DAA2A4 A4AF401E 0100 173 .QUAD ^X90DAA2A4A4AF401E : 2^(15/16)
00000000 00004020 0108 174 .QUAD ^X000000000000004020 : 2^(16/16)
0110 175
      59FC33E3 0110 176 EXPTAB: .LONG ^X59FC33E3
      00663876 0114 177 .LONG ^X00663876
      72183CB1 0118 178 .LONG ^X72183CB1
      9625B19D 011C 179 .LONG ^X9625B19D
      00000004 0120 180 EXPLEN = <.-EXPTAB>/4
```

0120 182 .SBTTL OTSS\$POWRR - REAL to REAL giving REAL result

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++
FUNCTIONAL DESCRIPTION:

OTSS\$POWRR - REAL result = REAL base ** REAL exponent

The REAL result is given by:

base	exponent	result
----	-----	-----
= 0	> 0	0.0
= 0	= 0	Undefined Exponentiation
= 0	< 0	Undefined Exponentiation
< 0	any	Undefined Exponentiation
> 0	> 0	$2^{\lceil \text{exp} * \log_2(\text{base}) \rceil}$
> 0	= 0	1.0
> 0	< 0	$2^{\lfloor \text{exp} * \log_2(\text{base}) \rfloor}$

Floating Overflow and Underflow can occur.

Undefined Exponentiation can occur if:

- 1) base is 0 and exponent is 0 or negative
- 2) base is negative

The basic approach to computing $x**y$ as $2^{\lceil y * \log_2(x) \rceil}$ is the following:

- Step 1: Compute $\log_2(x)$ to sufficient precision to guarantee an accurate final result (see below.)
- Step 2: Compute $y * \log_2(x)$ to at least the accuracy that $\log_2(x)$ was computed.
- Step 3: Evaluate $2^{\lceil y * \log_2(x) \rceil}$ accurate to the precision of the datatype in question.

To determine the accuracy to which $\log_2(x)$ must be computed to, write $y * \log_2(x)$ as $I + h$, where I is the integer closest to $y * \log_2(x)$, and $h = y * \log_2(x) - I$ (Note that $|h| \leq 1/2$.) Then

$$2^{\lceil y * \log_2(x) \rceil} = 2^{(I + h)} = (2^I) * (2^h).$$

Since the factor 2^I can be incorporated into the final result by an integer addition to the exponent field, we can assume that the multiplication by 2^I incurs no error. Thus the total error in the final result is determined by how accurately 2^h can be computed. If the final result has p fraction bits, we would like h to have at least p good bits. In fact it would be nice if h had a few extra guard bits, say 4. Consequently, we would like h to be accurate to $p + 4$ bits.

Let e be the number of bits allocated to the exponent field of the data type in question. If I requires more than e bits to represent, then overflow or underflow will occur. Therefore if the product $y * \log_2(x)$ has $e + p + 4$ good bits, the final result will be accurate. This requires that $\log_2(x)$ be computed to at least $p + e + 4$ bits.

0120 239 : Since log2(x) must be computed to more bits of precision than is available
0120 240 : in the base data type, either the next level of precision or multi-precision
0120 241 : arithmetic must be used. We begin by writing
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$$\log_2(x) = \log_2(b) + \sum_{n=0}^{\infty} c(2n+1)z'^{2n+1}$$

Where $c(1) = 1$, and $z' = (2/\ln 2)[(z-b)/(z+b)]$. Hence

$$\begin{aligned} \log_2(x) &= \log_2(b) + z' + \sum_{n=1}^{\infty} c(2n+1)z'^{2n+1} \\ &= \log_2(b) + z' + p(z'). \end{aligned}$$

Note that if $p(z')$ is computed to p bits, and $\log_2(b) + z'$ is computed to $p+e+4$ bits and overhangs $p(z')$ by $e+4$ bits, the required accuracy will be achieved. Consequently, the essential tricks, are to pick b such that the overhang can be achieved and to compute $\log_2(b) + z'$ to $p + e + 4$ bits.

CALLING SEQUENCE:

power.wf.v = OTSS\$POWRR (base.rf.v, exponent.rf.v)

INPUT PARAMETERS:

Base and exponent parameters are call by value

IMPLICIT INPUTS:

none

OUTPUT PARAMETERS:

none

IMPLICIT OUTPUTS:

none

FUNCTIONAL VALUE:

OTSS\$POWRR - REAL base ** REAL power

SIDE EFFECTS:

SIGNALS MTH\$K_FLOOVEMAT if floating overflow.
SIGNALS MTH\$K_FLOUNDMAT if floating underflow.
SIGNALS MTH\$K_UNDEXP (82 = 'UNDEFINED EXPONENTIATION') if
1) base is 0 and exponent is 0 or negative
2) base is negative

```

001C 0120 295      .ENTRY OTSS$POWRR, ACMASK      ; standard call-by-reference entry
      0122 296      ; disable DV (and FU)
      0122 297
      0122 298
      0122 299      : Move x to R0. If x < 0, or x = 0 and y <= 0, return 'UNDEFINED
      0122 300      : EXPONENTIATION' error condition, otherwise attempt to compute x**y
      0122 301
      0122 302
      50 04 AC 50 0122 303      MOVF      base(AP), R0      ; R0 <-- x
      1A 14 0126 304      BGTR      DEFINED      ; If x > 0 attempt to compute x**y
      07 19 0128 305      BLSS      UNDEFINED      ; Branch to error code for x < 0
      51 08 AC 50 012A 306      MOVF      exp(AP), R1      ; R1 <-- y (Note that x = 0)
      01 15 012E 307      BLEQ      UNDEFINED      ; Branch to error condition if y <= 0
      0130 308
      0130 309
      0130 310      : If processing continues here, this implies that x = 0 and y > 0. Return
      0130 311      : with x**y = 0
      0130 312
      0130 313
      04 0130 314      RET      ; Return
      0131 315
      0131 316
      0131 317      : If processing continues here, this implies that an undefined exponentiation
      0131 318      : was attempted. Signal error and return
      0131 319
      0131 320
      0131 321      UNDEFINED:
      50 8000 8F 3C 0131 322      MOVZWL  #^X8000, R0      ; R0 <-- Reserved operand
      7E 00 8F 9A 0136 323      MOVZBL  #MTH$K UNDEXP, -(SP) ; Put error code on stack
      00000000'GF 01 FB 013A 324      CALLS  #1, G^MTH$$SIGNAL ; Convert error number to 32 bit
      0141 325      ; condition code and signal error.
      0141 326      ; NOTE: Second argument is not re-
      0141 327      ; quired since there is no JSB entry.
      04 0141 328      RET      ; Return
      0142 329
      0142 330
      0142 331      : If processing continues here will attempt to compute x**y as 2^[y*log2(x)].
      0142 332      : We begin by determining an integer k and a real number f such that x = 2^k*f,
      0142 333      : and 1 <= f < 2.
      0142 334
      0142 335
      0142 336      DEFINED:
      54 50 FFFF807F 8F CB 0142 337      BICL3  #^XFFF807F, R0, R4 ; R4 <-- 2^7*(biased exponent of x)
      54 00004080 8F C2 014A 338      SUBL  #^X4080, R4 ; R4 <-- 2^7*k = 2^7*(exponent_of_x - 1)
      50 54 C2 0151 339      SUBL  R4, R0 ; R0 <-- f = 2*(fraction field of x)
      0154 340
      0154 341
      0154 342      : We are now ready to compute log2(x). This computation is based on the
      0154 343      : following identity:
      0154 344
      0154 345      : 
$$\log_2(2^k f) = k + \log_2(a) + \frac{2}{\ln(2)} \sum_{j=1}^{\infty} \frac{1}{2j+1} z^{2j+1}, \text{ where } z = \frac{f-a}{f+a}.$$

      0154 346
      0154 347
      0154 348
      0154 349      : We begin by determining a as b^i, where b = 2^(1/16) and i is between 0
      0154 350      : and 16 inclusive. Specifically i is chosen by table look-up so that
      0154 351      : the magnitude of z is minimized. Since log2(a) = i/16, we may write

```



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0154 352 ::
0154 353 ::      log2(2^k*f) = k + i/16 + z*p(z^2).
0154 354 ::
0154 355 ::      Note that in order to insure an accurate result, log2(2^k*f) must be computed
0154 356 ::      accurately to 36 bits. This will require some double precision arithmetic.
0154 357 ::
0154 358 ::
0154 359 EVAL_LOG2:
52 50 FFFFFFF80 8F CB 0154 360 BICL3 #XFFFFFF80, R0, R2 ; R2 <-- index to INDEX table
52 52 FE9F CF42 90 015C 361 MOVB INDEX[R2], R2 ; R2 <-- i*2^3
52 52 54 52 C0 0162 362 ADDL R2, R4 ; R4 <-- 2^7*(k + i/16)
52 52 FD 8F 9C 0165 363 ROTL #-3, R2, R2 ; R2 <-- i
016A 364 ; R2 will be multiplied by 2^3 by
016A 365 ; table references like the line below.
016A 366 ; The linker will cause an error if
016A 367 ; () are used instead of [] for these
016A 368 ; table references.
52 50 50 50 99FD 016A 369 CVTFG R0, R0 ; R0/R1 <-- f
52 50 FF14 CF42 43FD 016E 370 SUBG3 A_TABLE[R2], R0, R2 ; R2/R3 <-- f - a (NOTE: result is
0176 371 ; exact, i.e. no roundoff error)
52 10 A0 0176 372 ADDW #X10, R0 ; R0/R1 <-- 2*f
52 52 42FD 0179 373 SUBG2 R2, R0 ; R0/R1 <-- f + a
52 50 46FD 017D 374 DIVG2 R0, R2 ; R2/R3 <-- z
0181 375
0181 376 ::
0181 377 ::      Compute 2^7*z*p(z^2) = z*(c0* + c2*z^2 + c4*z^4), where the c's are chosen
0181 378 ::      to minimize the absolute error of the approximation
0181 379 ::
0181 380 ::
7E 53 FFFF1FFF 8F CB 0181 381 BICL3 #XFFF1FFF, R3, -(SP) ; prepare to save R2 and to clear
7E 52 D0 0189 382 MOVL R2, -(SP) ; the rounding bit in order to
7E 8E 33FD 018C 383 CVTGF (SP)+, -(SP) ; to form a truncated CVTGF
51 8E 6E 45 0190 384 MULF3 (SP), (SP)+, R1 ; R1 <-- z^2
50 51 C0234393 8F 45 0194 385 MULF3 #C4, R1, R0 ; R0 <-- c4*z^2
50 50 384F43F6 8F 40 019C 386 ADDF #C2, R0 ; R0 <-- c2 + c4*z^2
50 51 44 01A3 387 MULF R1, R0 ; R0 <-- c2*z^2 + c4*z^4
50 50 99FD 01A6 388 CVTFG R0, R0 ; R0/R1 <-- c2*z^2 + c4*z^4
50 FED1 CF 40FD 01AA 389 ADDG2 C0, R0 ; R0/R1 <-- c0 + c2*z^2 + c4*z^4
52 50 44FD 01B0 390 MULG2 R0, R2 ; R2/R3 <-- 2^7*z*p(z*z)
01B4 391
01B4 392 ::
01B4 393 ::      Compute log2(x) = k + i/16 + z*p(z)
01B4 394 ::
01B4 395 ::
50 54 4EFD 01B4 396 CVTLG R4, R0 ; Convert 2^7*(k + i/16) to double
52 50 40FD 01B8 397 ADDG2 R0, R2 ; R2/R3 <-- 2^7*log2(x)
01BC 398
01BC 399 ::
01BC 400 ::      We can now compute x**y as 2^[y*log2(x)]. We begin by computing
01BC 401 ::      y*log2(x). (Note that R1 = 0.)
01BC 402 ::
01BC 403 ::
50 08 AC 50 01BC 404 MOVF exp(AP), R0 ; R0/R1 <-- y
50 50 99FD 01C0 405 CVTFG R0, R0
01C4 406
01C4 407 ::      Test for the possibility of overflow in the computation of y*w1.
01C4 408 ::      This will occur if the exponent of y plus the exponent of w1 is greater
```



```

01C4 409 ; than 127.
01C4 410 ;
7E 50 0B 04 EF 01C4 411 EXTZV #4, #11, R0, -(SP) ; biased exp of y
6E 0400 8F A2 01C9 412 SUBW2 #X400, (SP) ; unbiased exp of y
54 52 0B 04 EF 01CE 413 EXTZV #4, #11, R2, R4 ; biased exp of 2^7*log2(x)
54 0400 8F A2 01D3 414 SUBW2 #X400, R4 ; unbiased exp of 2^7*log2(x)
54 54 8E C0 01D8 415 ADDL2 (SP)+, R4 ; unbiased exp of 2^7*log2(x)*y
54 007F 8F B1 01DB 416 CMPW #X7F, R4 ; largest unbiased exp possible is 127
03 18 01E0 417 BGEQ NO_SYS_OVERFLOW
008C 31 01E2 418 BRW Y_TIMES_W1_OVER
01E5 419 NO_SYS_OVERFLOW:
52 50 44FD 01E5 420 MULG2 R2, R2 ; R2/R3 <-- 2^7*y*log2(x)
01E9 421
01E9 422
01E9 423 ; The next step in computing 2^[y*log2(x)] is to write y*log2(x) as
01E9 424 y*log2(x) = I + j/16 + g/16,
01E9 425 where I is an integer, j is an integer between 0 and 15 inclusive, and
01E9 426 g is a fraction in the interval [-1/2, 1/2)
01E9 427
01E9 428
01E9 429
01E9 430
7E 53 FFFF1FFF 8F CB 01E9 431 BICL3 #XFFFF1FFF, R3, -(SP)
7E 52 D0 01F1 432 MOVL R2, -(SP)
54 54 00004DC0 8F 41 01F4 433 CVTGF (SP)+, R4
50 54 00004DC0 8F 41 01F8 434 ADDF3 #X4DC0, R4, R0 ; 3*2^5 is used in this truncation process
0200 435 ; to avoid a possible normalization
0200 436 ; that could occur if the number is neg
50 00004DC0 8F 42 0200 437 SUBF #X4DC0, R0 ; R0/R1 <-- 2^7(I + j/16) in double
50 50 99FD 0207 438 CVTFG R0, R0
52 50 42FD 020B 439 SUBG2 R0, R2 ; R2/R3 <-- 2^7(g/16)
54 50 49FD 020F 440 CVTFG R0, R4 ; R4 <-- 2^7(I + j/16) in integer
52 1D 0213 441 BVS EXCEPTION_1 ; Branch if !I is too large
0215 442
0215 443
0215 444 ; We can now compute
0215 445 x*y = 2^[y*log2(x)] = 2^[I + j/16 + g/16]
0215 446 = (2^I)*[A*(B+1)] = 2^I*[A + A*B], where
0215 447
0215 448
0215 449 A = 2^(j/16) is obtained from the A_TABLE and B = 2^(g/16) - 1 is obtained
0215 450 by a min/max approximation whose coefficients compensate to the factor of
0215 451 2^7.
0215 452
0215 453
0215 454
53 FFFF1FFF 8F CA 0215 455 BICL2 #XFFFF1FFF, R3
52 52 33FD 021C 456 CVTGF R2, R2
FEEA CF 03 52 55 0220 457 POLYF R2, #EXPLEN-1, EXPTAB ; R0 <-- B = 2^(g/16) - 1
52 54 FFFFFFF80 8F CB 0226 458 BICL3 #XFFFFFF80, R4, R2 ; R2 <-- index into A_TABLE table
52 52 FD 8F 9C 022E 459 ROTL #-3, R2, R2 ; R2 <-- index into A_TABLE table
52 52 FE50 CF42 7D 0233 460 MOVQ A_TABLE[R2], R2 ; R2/R3 <-- A = 2^(j/16)
7E 53 FFFF1FFF 8F CB 0239 461 BICL3 #XFFFF1FFF, R3, -(SP)
7E 52 D0 0241 462 MOVL R2, -(SP)
7E 8E 33FD 0244 463 CVTGF (SP)+, -(SP)
50 8E 44 0248 464 MULF2 (SP)+, R0 ; R0 <-- A*B
50 50 99FD 024B 465 CVTFG R0, R0

```

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50 52 40FD 024F 466      ADDG2  R2, R0      ; R0/R1 <-- A + A*B
50 50 33FD 0253 467      CVTGF  R0, R0      ; R0 <-- 2^[(j + g)/16]
54 007F 8F AA 0257 468      BICW2  #^X7F, R4    ; R4 = 2^7*I
50 54 A0 025C 469      ADDW2  R4, R0      ; R0 <-- 2^I*2^[(j+g)/16]
007F 8F 50 B1 025F 470      CMPW  R0, #^X7F    ; test for over/underflow
07 15 0264 471      BLEQ  EXCEPTION_2    ; see what exception is if neg or = 0
04 04 0266 472      RETURN: RET          ; otherwise return result in R0
0267 473
0267 474
0267 475      ; Handlers for software detected over/underflow conditions follow
0267 476
0267 477
0267 478      EXCEPTION 1:
50 53 0267 479      TSTF  R0      ; if big ARG > 0 goto overflow
1D 18 0269 480      BGEQ  OVER    ; handler, otherwise go to
08 11 026B 481      BRB  UNDER   ; underflow handler
026D 482      EXCEPTION 2:
54 B5 026D 483      TSTW  R4      ; test sign of I; if I >= 0
17 18 026F 484      BGEQ  OVER    ; go to overflow handler
0271 485
0271 486
0271 487      ; y*w1 would have caused a hardware system floating overflow error. If y<0,
0271 488      ; then we should return a result of 0 since result = 2^(y*(w1+w2)). Note,
0271 489      ; y can not be zero.
0271 490
0271 491
0271 492      Y_TIMES_W1_OVER:
50 53 0271 493      TSTF  R0      ; if y < 0 no overflow is needed
13 14 0273 494      BGTR  OVER    ; overflow for y > 0
0275 495
0275 496
0275 497      ; Underflow; if user has FU set, signal error. Always return 0.0
0275 498
0275 499
0275 500      UNDER:  CLRL  R0      ; R0 = result.
0B 04 AD 06 E1 0277 501      BBC  #6, SF$W_SAVE_PSW(FP), 2$
027C 502
027C 503      MOVZBL #MTH$K_FLOUNDMAT, -(SP) ; has user enabled floating underflow?
7E 00'8F 9A 027C 503      ; trap code for hardware floating
0280 504      ; underflow. Convert to MTH$FLOUNDMAT
0280 505      ; (32-bit VAX-11 exception code)
00000000'GF 01 FB 0280 506      CALLS #1, G^MTH$$SIGNAL ; signal condition
04 04 0287 507 2$: RET          ; return
0288 508
0288 509
0288 510      ; Signal floating overflow, return reserved operand, -0.0
0288 511
0288 512
0288 513      OVER:  MOVZBL #MTH$K_FLOOVEMAT, -(SP) ; Move overflow code to stack
50 01 0F 79 0288 513      ASHQ  #15, #T, R0 ; R0 = result = reserved operand -0.0.
028C 514      ; R0 will be copied to signal mechanism
0290 515      ; vector (CHF$MCH_R0/R1) so it can be
0290 516      ; fixed up by any error handler
00000000'GF 01 FB 0290 517      CALLS #1, G^MTH$$SIGNAL ; signal condition
04 04 0297 518      RET          ; return - R0 restored from CHF$MCH_R0/R1
0298 519
0298 520
0298 521      .END

```

UVX\$POWRR
Symbol table

- REAL ** REAL power routine

G 1

16-SEP-1984 02:07:47
6-SEP-1984 11:29:13

VAX/VMS Macro V04-00
[MTHRTL.SRC]UVXPOWRR.MAR;1

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ACMASK	= 0000001C		
A TABLE	00000088	R	02
BASE	= 00000004		
CO	00000080	R	02
C2	= 384F43F6		
C4	= C0234393		
DEFINED	00000142	R	02
EVAL LOG2	00000154	R	02
EXCEPTION_1	00000267	R	02
EXCEPTION_2	0000026D	R	02
EXP	= 00000008		
EXPLEN	= 00000004		
EXPTAB	00000110	R	02
INDEX	00000000	R	02
MTH\$SIGNAL	*****	X	00
MTH\$K_FLOOVEMAT	*****	X	00
MTH\$K_FLOUNDMAT	*****	X	00
MTH\$K_UNDEXP	*****	X	00
NO SYS OVERFLOW	000001E5	R	02
OT\$POWRR	00000120	RG	02
OVER	00000288	R	02
RETURN	00000266	R	02
SFSW_SAVE_PSW	= 00000004		
UNDEFINED	00000131	R	02
UNDER	00000275	R	02
Y_TIMES_W1_OVER	00000271	R	02

+-----+
! Psect synopsis !
+-----+

PSECT name	Allocation	PSECT No.	Attributes															
. ABS .	00000000 (0.)	00 (0.)	NOPIC	USR	CON	ABS	LCL	NOSHR	NOEXE	NORD	NOWRT	NOVEC	BYTE					
\$AB\$	00000000 (0.)	01 (1.)	NOPIC	USR	CON	ABS	LCL	NOSHR	EXE	RD	WRT	NOVEC	BYTE					
_OT\$CODE	00000298 (664.)	02 (2.)	PIC	USR	CON	REL	LCL	SHR	EXE	RD	NOWRT	NOVEC	LONG					

+-----+
! Performance indicators !
+-----+

Phase	Page faults	CPU Time	Elapsed Time
Initialization	35	00:00:00.10	00:00:00.88
Command processing	107	00:00:00.56	00:00:02.62
Pass 1	128	00:00:01.87	00:00:05.91
Symbol table sort	0	00:00:00.04	00:00:00.04
Pass 2	104	00:00:01.15	00:00:05.10
Symbol table output	4	00:00:00.04	00:00:00.21
Psect synopsis output	2	00:00:00.03	00:00:00.03
Cross-reference output	0	00:00:00.00	00:00:00.00
Assembler run totals	382	00:00:03.79	00:00:14.80

The working set limit was 1050 pages.
9361 bytes (19 pages) of virtual memory were used to buffer the intermediate code.
There were 10 pages of symbol table space allocated to hold 54 non-local and 1 local symbols.
521 source lines were read in Pass 1, producing 13 object records in Pass 2.

UVX\$POWRR
VAX-11 Macro Run Statistics

- REAL ** REAL power routine

H 1

16-SEP-1984 02:07:47 VAX/VMS Macro V04-00
6-SEP-1984 11:29:13 [MTHRTL.SRC]UVXPOWRR.MAR;1

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(5)

8 pages of virtual memory were used to define 7 macros.

+-----+
! Macro library statistics !
+-----+

Macro library name

Macros defined

_S255\$DUA28:[SYSLIB]STARLET.MLB;2

4

88 GETS were required to define 4 macros.

There were no errors, warnings or information messages.

MACRO/ENABLE=SUPPRESSION/DISABLE=(GLOBAL,TRACEBACK)/LIS=LIS\$:UVXPOWRR/OBJ=OBJ\$:UVXPOWRR MSRC\$:UVXPOWRR/UPDATE=(ENHS:UVXPOWRR)

0265 AH-BT13A-SE
VAX/VMS V4.0

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0266 AH-BT13A-SE
VAX/VMS V4.0

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NCP
MRP

LUXSORT2
LIS

LUXSORT
LIS

NCPDEF
SOL

LUXSINCOS
LIS

NMADEF
SOL

NCP